Lewknor Church of England Primary School

Calculation Policy

Introduction:

Children are introduced to the processes of calculation through practical, oral and mental activities. As they begin to understand the underlying ideas, they develop ways of recording to support their thinking and calculation methods, so that they develop both **conceptual understanding** and **fluency** in the fundamentals of mathematics. Whilst interpreting signs and symbols involved with calculation, orally in the first instance, children use models and images to support their mental and written methods of calculation. As children's mental methods are strengthened and refined they begin to work more efficiently, which will support them with using succinct written calculation strategies as they are developed.

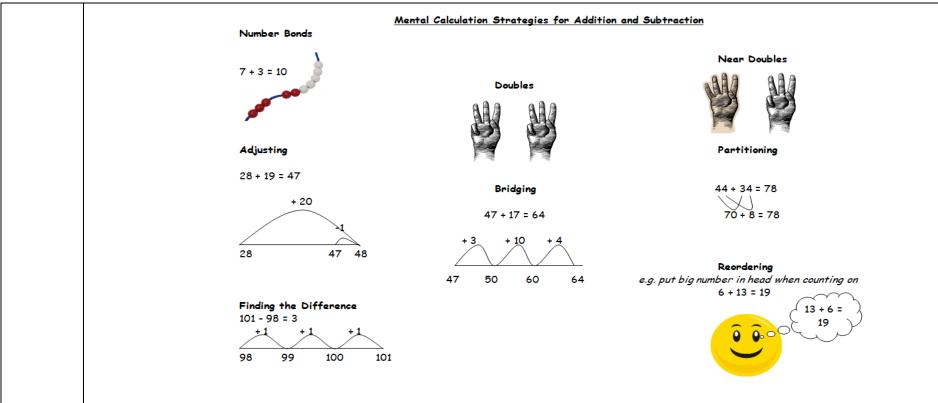
The ability to calculate mentally forms the basis of all methods of calculation and has to be maintained and refined. A good knowledge of numbers or a 'feel' for numbers is the product of structured practice through progression in relevant practical maths experiences and visual representations.

By the end of Year 6, children will be equipped with efficient mental and written calculation methods, which they use with fluency. Decisions about when to progress should always be based on the security of pupils' understanding and their readiness to progress to the next stage. At whatever stage in their learning, and whatever method is being used, children's strategies must still be underpinned by a secure understanding and knowledge of number facts that can be recalled fluently.

The overall aims are that when children leave primary school they:

- Are able to recall number facts with fluency, having developed conceptual understanding through being able to visualise key ideas such as those related to place value through experience with practical equipment and visual representations;
- Make use of diagrams and informal notes to help record steps and part answers when using mental methods that generate more information than can be kept in their heads;
- Have an efficient, reliable, written method of calculation for each number operation that they can apply with confidence when undertaking calculations that they cannot carry out mentally;
- Are able to make connections between all four number operations, understanding how they relate to one another, as well as how the rules and laws of arithmetic can be applied.

Addition:



	Counting	Mental Rapid recall strategies		Written calculation and appropriate models and images to support conceptual understanding				
Stage 1:	Count in ones to and across 100 forwards and backwards starting from	apparatus to explore numbers addition as the inverse of numbers up	totalling numbers up	 Combining two groups: Children develop a mental picture of the number system for use with calculation. A range of key models and images support this, alongside practical equipment. 	123456789 ••• • • 3 + 2 = 5			
	0, 1 and other numbers. Count in		Use structured apparatus –	Teachers model use of number tracks to count on or line up	'eight add two more makes ten'			

	multiples of two, five and ten.	3 2 4 add 1 is 5 5 subtract 4 leaves 1	i.e. Numicon, tens frames, abaci, etc.	counters/objects along the number track. This is a precursor to use of a fully numbered number-line.	'one more than four is five'
Stage 2:	Continue practicing above skills. Count in steps of 2, 3 and 5 forwards and backwards to and from zero. Count in tens from any number – link to coins in a piggy bank as well as a number square.	Reorder numbers when adding, i.e. start with largest number, find bonds, etc. Add doubles and derive near doubles. Round numbers to the nearest 10.	Recall addition facts for all numbers to 20.	 Counting on from any number: Children begin to use numbered lines to support their own calculations, initially counting in ones before beginning to work more efficiently. Counting on from the largest number: Children reorder calculations to start with the largest number. 	Number line with all numbers labelled 0 1 2 3 4 5 6 7 8 9 10 11 12 18 + 5 to 18 19 20 21 22 23 Use of questions such as: 'How might I rearrange these to find the total?'

Ctage 2:	Continue	Dartitioning by	Connoct	Evpanded herizontal addition:	Add
Stage 3:	Continue	Partitioning by	Connect	Expanded horizontal addition:	Add
	practicing	bridging	pairs	Add numbers using structured	
	above skills.	through 10	totalling ten	apparatus to support	00000
	Count from 0	and multiples	to pairs of	understanding of place value.	
	in multiples of	of 10 when	multiples of	Make connections between	and
	4, 8, 50 and	adding.	10 totalling	partitioning both numbers using	
	100. Count on	Adjusting	100.	structured apparatus and partition	
	by 10 or 100	when adding		the second number only using a	000000
	from any two	11 or 9 to a		number line.	
	digit number.	number.			By partitioning and recombining
	Link to	Relating			30+ 40 = 70
	counting	inverse			5 + 7 = 12
	stick:	number			70 + 12 = 82
	counting	operations –	Use 10ps in		, 0 . 12
	forwards and	using	tens frame.		35 + 47
	backwards	structured	Recall pairs		+30
	flexibly.	apparatus to	of two-digit		+3 +2
	Count up and	explore and	numbers		
	down in	understand	with a total		
	tenths –	that	of 100, i.e.		47
	linking to	subtraction	32 + ? =		
	visual image.	undoes	_		
	visuai iiilage.	addition.	100.		
Stage 4:	Continue	Bridging	As above.	Expanded horizontal method,	It is crucial that empty number lines are
	practicing	through 60 for	Use known	leading to columnar addition:	kept as well as using more formal written
	previous	time, i.e. 70	facts and	Written recording should follow	calculation methods.
	skills. Count	minutes = 1	place value	teacher modelling around the size	
	forwards and	hour and 10	to derive	of numbers and place value using	
	backwards	minutes.	new ones,	a variety of concrete materials,	
	from 0 in	Rounding any	i.e. `If I	e.g. straws, Numicon, Dienes and	
	multiples of 6,	number to the	know 8 + 3	place-value cards.	
	7, 9, 25 and	nearest 10,	= 11, I also	Teachers model how numbers can	
	1000 using	100 or 1000.	know 0.8 +	be partitioned into tens and ones,	
	counting	Rounding	0.3 = 1.1	as well as in different ways,	
	sticks,	numbers with	and 8/100 +	e.g. 20 + 5	
	number lines,	one decimal	3/100 =	10 + 15	
	Transport in ico,	one decimal	J/ 100 -	10 1 13	

number
squares, etc.
Count up and
down in
tenths,
hundredths
and simple
fractions
using models
and images,
i.e. Dienes
equipment,
counting
stick, ITPs.

place to nearest whole number. Explore inverse as a way to derive new facts and to check accuracy of answers. 11/100.'
Sums and differences of pairs of multiples of 10, 100 or 1000.
Addition doubles of numbers to 100.
Pairs of fractions totalling 1.

 As children move towards using a columnar method, links continue to be made with earlier models and images, including the number line.

Counting on in tens and ones to solve an addition calculation:

34 + 23 = 57 +10 +10 +1 +1 +1 10 +10 34 44 54 55 56 57

Counting on more efficiently:

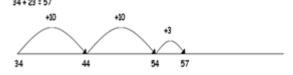
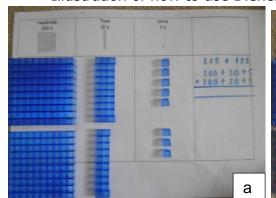
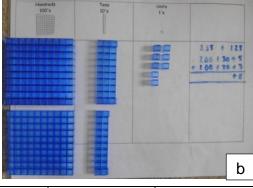
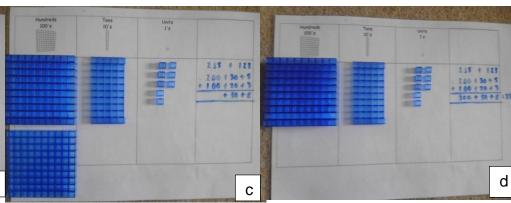


Illustration of how to use Dienes equipment to ensure children have an understanding of place value when using columnar addition.







Stage 5:

Count forwards and backwards in steps of powers of 10 for any given number up to one million. Continue to count

Use apparatus and knowledge of place value to add decimals, i.e. 3.8 + 2.5 = 5 + 1.3 Reorder increasingly complex

Continue to practice previous stage and make links between known facts and addition pairs for fractions,

Expanded vertical method, leading to columnar addition:

- Teachers model a column method that records and explains partial mental methods.
- There remains an emphasis on the language of calculation, e.g. 'Forty plus seventy equals onehundred and ten.'... 'Seven add six equals thirteen.' ...before

Informal columnar:

Adding the tens first:

47
+ 76

Adding the ones first:

	forwards and backwards in simple fractions. Count forward and backwards in appropriate decimals and percentages.	calculations, i.e. $1.7 + 2.8$ + 0.3 = 1.7 + 0.3 + 2.8 Compensating - i.e. $405 +399 \rightarrow add400$ and then subtract 1.	percentages and decimals Doubles and halves of decimals, i.e. half of 5.6, double 3.4. Sums and differences of decimals, i.e. 6.5 + 2.7	recombining numbers. Teachers also model the language of: `Four tens add seven tens total eleven tens or 110.' • Teachers similarly advance to model the addition of two 3-digit numbers with the expectation that as children's knowledge of place value is secured, they become ready to approach a formal compact method.	47 + 76 13 110 123
Stage 6:	Continue to practice previous skills. Count forwards and backwards in simple fractions, decimals and percentages.	Bridging through decimals, i.e. $0.8 + 0.35 = 0.8 + 0.2 + 0.15$ using empty number lines. Partitioning using near doubles, i.e. $2.5 + 2.6 = 5 + 0.1$ Reorder decimals, i.e. $4.7 + 5.6 - 0.7$ as $4.7 - 0.7 + 5.6 = 4 + 5.6$.	Ensure all children are confident recalling basic facts to 20 and deriving facts using place value. Make links between decimals, fractions and percentages.	 Columnar addition (formal written method): The concept of exchange is introduced through continued use of practical equipment (manipulatives). Teachers model: "I have two tens and five ones, which need adding to four tens and seven ones." "I add five ones to seven ones, which gives me twelve ones." "I exchange ten of my twelve ones for a ten counter." "I add my three tens and four tens to make seven tens." "Altogether, I have seven tens and two ones." Teachers similarly advance to model the addition of two 3-digit numbers, e.g. 	Pupils to be encouraged to consider mental strategies first. Formal columnar: 25 +47 Tens Ones 25 +47 25 +47 2 1 1 1 1 1 1 1 1 1 1 1 1

			Tens	Ones	
		587	10 10		
		+ 475 1062		0 0	
		1062		1 1	
		1 1	10 10		
			0 0		
			25 <u>+47</u> 2		
			+4 /_		
			1		
			Tens	Ones	
			10 0		
			10	1 1	
			10 10		
			0 10		
			25		
			25 + 47		
			+4 /		
			25 +47 -72		
			Tens	Ones	
			10 10		
			10 10		
			0 0 0 0 0 0	1 1	

Subtraction:

	Counting	Mental strategies	Rapid Recall	Written calculation as conceptual understan	nd appropriate models and images to support
Stage 1:	Count in ones to and across 100, forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten.	Pupils use apparatus to explore addition as the inverse of subtraction: . 'four add one is five.' 'five subtract four leaves one'	Rapid recall of subtraction facts for numbers up to 10. Use structured apparatus, i.e. Numicon, tens frames, abaci etc.	Subtraction as taking away from a group: • Children develop a mental picture of the number system for use with calculation. A range of key models and images support this, alongside practical equipment. • Teachers model use of number tracks to count back or remove counters/objects from the number track or set. This is a precursor to use of a fully numbered number-line.	1234567890 *Six take away two leaves four' 'one less than six is five'
Stage 2:	Continue practicing above skills. Count in	Bridging through two digit numbers, i.e. 24 – 19 = 19 + 1 + 4 using number	Recall subtraction (and addition)	Subtracting by counting back and on: • Children begin	Number line with all numbers labelled 0 1 2 3 4 5 6 7 8 9 10 11 12

	steps of 2, 3 and 5, forwards and backwards to and from zero. Count in tens from any number – link to coins in a piggy bank as well as a number square.	lines. Subtracting 11 by subtracting 10 and then 1 more. Move to subtracting 9 by subtracting 10 and adding 1 using apparatus.	facts for all numbers to 20.	to use numbered lines to support their own calculations, initially counting back in ones before beginning to work more efficiently.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Stage 3:	Continue practicing above skills. Count from 0 in multiples of 4, 8, 50 and 100. Count on and back by 10 or 100 from any two digit number. Link to counting stick counting forwards and backwards flexibly. Count up and down in tenths —	Partitioning by bridging through 10 and multiples of 10 when subtracting. Continue to practice adjusting when subtracting 11 or 9 from a number. Relating inverse number operations – use structured apparatus to explore and understand that subtraction undoes addition.	Connect subtractions from ten to subtractions from multiples of 10 totalling 100. Use 10ps in tens frame. Subtract two digit numbers from 100 i.e. ? = 100 - 78	Finding the difference: • Teachers model how to find the difference when two numbers are relatively 'close together.' • Initially children compare two sets before moving on to a number line comparison. • Pupils are taught to choose whether to count on or back depending on which is more efficient.	Comparing two sets: comparison or difference. Finding the difference on a number line. Note: Finding the difference is often the most efficient way of solving a subtraction problem, e.g. 61 – 59 2,003 – 1,997

	linking to visual image.				
Stage 4:	Continue practicing of previous skills. Count forwards and backwards from 0 in multiples of 6, 7, 9, 25 and 1000 using counting sticks, number lines, number squares, etc. Count up and down in tenths, hundredths and simple fractions using models and images, i.e. Dienes equipment, counting stick, ITPs.	Bridging through 60 for time, i.e. 70 minutes = 1 hour and 10 minutes Rounding any number to the nearest 10, 100 or 1000. Rounding numbers with one decimal place to nearest whole number. Explore inverse as a way to derive new facts and to check accuracy of answers. Use apparatus and	As above. Use known facts and place value to derive new ones, i.e. 'If I know 11 - 3 = 8, I also know 1.1 - 0.3 = 0.8 and 8/100 - 3/100 = 5/100.' Sums and differences of pairs of multiples of 10, 100 or 1000. Subtraction of fractions totalling 1, i.e. 1 - 0.3 = 0.7	Subtracting TU - U and TU - TU:	Use empty number lines to find the difference by bridging through multiples of ten. 74 -27 = 47 +3 +4 The subtract by starting with the first number and partitioning the second, i.e. 74 - 27 74 - 20 = 54 54 - 4 = 50 50 - 3 = 47 Children should continue to use empty number lines
5:	forwards and backwards in steps of	knowledge of place value to subtract decimals, i.e. 3.8 -	practice previous stage and	column method, including expanded method:	and use more formal written methods when numbers become too big or complex.

	powers of 10 for any given number up to one million. Continue to count forwards and backwards in simple fractions. Count forward and	$2.5 = 1.3$ Reorder increasingly complex calculations, i.e. $1.7 - 5 - 0.7 = 1.7 - 0.7 - 5$. Compensating – i.e. $405 - 399 \rightarrow$ subtract 400 and then add 1 .	make links between known facts and addition pairs for fractions, percentages and decimals. Doubles and halves of decimals, i.e. half of	•	Written recording should follow teacher modelling around the size of numbers and place value using a variety of concrete materials, e.g. straws, Numicon, Dienes and	Counting back in tens and ones to solve an addition calculation: 47 - 23 = 24 Counting back more efficiently: 47 - 23 = 24 Counting back more efficiently:
					•	
					,	Counting back more efficiently:
		subtract 400 and				47 - 23 = 24
9	simple	then add 1.	Doubles and		materials, e.g.	-10 -10
f	fractions.		halves of		straws,	
(Count		,		Numicon,	24 27 37 47
f	forward and		i.e. half of		Dienes and	
	backwards in		5.6, double		place-value	
	appropriate		3.4.		cards.	
(decimals and		Sums and			
	percentages.		differences			
			of decimals,			
			i.e. 6.5 +			
			2.7			

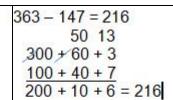
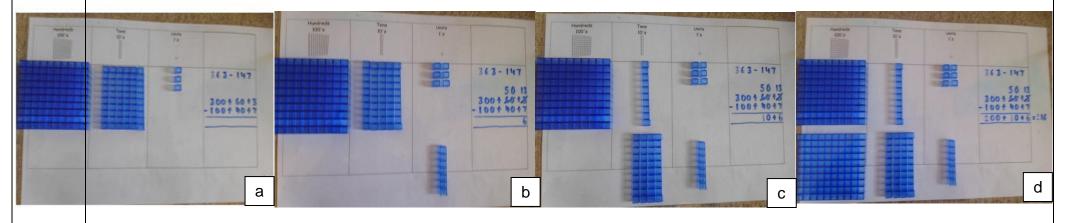


Illustration of how to use Dienes equipment to ensure children understand transference of numbers when using columnar subtraction.



Stage 6:

Continue to practice previous skills.
Count forwards and backwards in simple fractions, decimals and percentages.

Bridging through decimals, i.e. 1.5 – 0.8 = 1.5 – 0.5 then -0.3 using empty number line.

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Ensure all children are confident recalling basic facts to 20 and

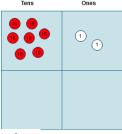
deriving using place value. Make links between decimals, fractions and percentages.

Second stage of column method:

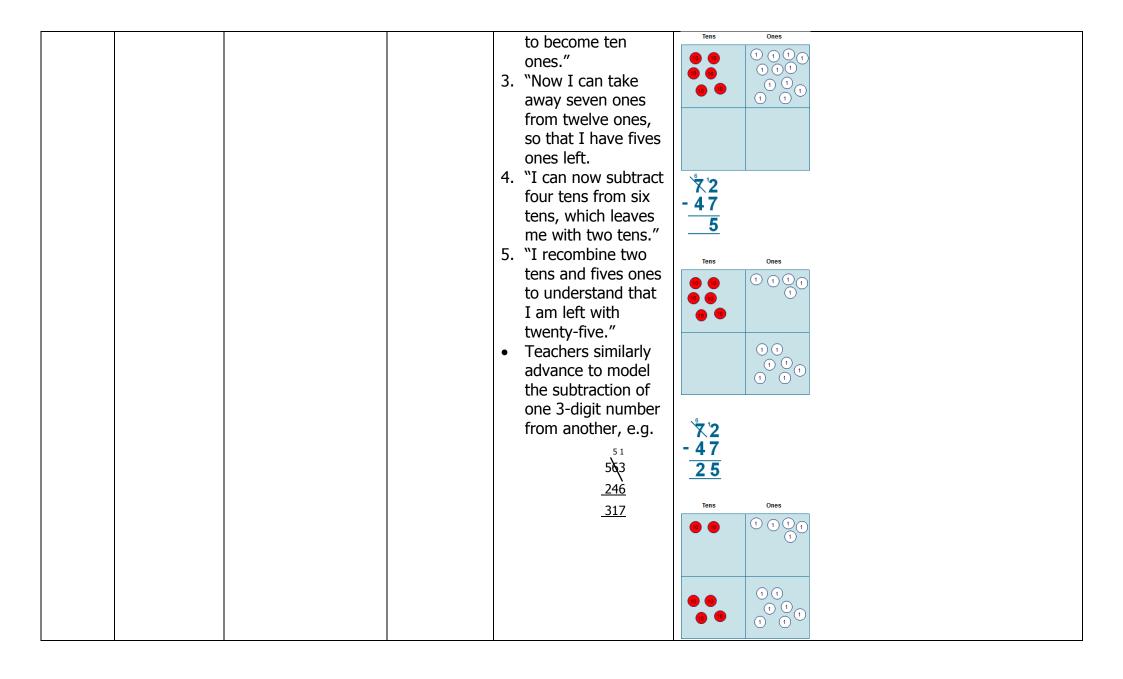
- The concept of exchange is introduced through continued use of practical equipment (manipulatives).
- Teachers model:
- 1. "I have seven tens and two ones. I need to subtract four tens and seven ones."
- 2. "At the moment, I cannot subtract seven ones from two ones, so I need to transfer one ten

Formal columnar:

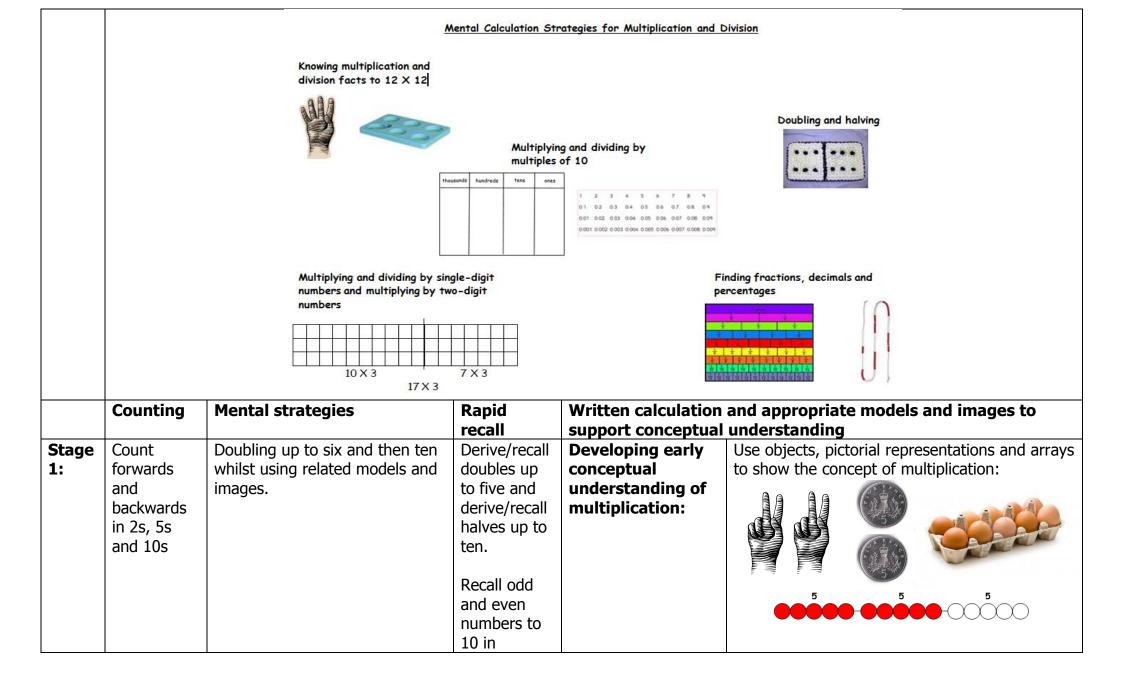








Multiplication:



			reference to structured apparatus.		
Stage 2:	Count forwards and backwards in 2s, 3s, 5s and 10s from zero.	Begin to understand and use inverse number operations: 10 2 5 Stories are used alongside a triad to help children understand links between number operations, e.g. "There are five pencils in two packs, which means that there are ten pencils altogether."	Derive/recall doubles up to ten and derive/recall halves up to twenty. Recall odd and even numbers to 20 in reference to structured apparatus. Recall & use multiplication facts for the 2X, 5X and 10X-tables.	Understanding multiplication as repeated addition: • Investigate multiplication as repeated addition, so that the law of cummutativity is understood. • Whilst arrays are also modelled explicitly at this stage, it is important to note that they will continue to be a key model at later stages, alongside more formal methods of calculation.	Arrays: 5 X 3 and Number lines: 6 X 4 = 24 So: 'Six taken four times"

Stage 3:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 8s and 10s from zero. Count up and down in tenths.	Use doubling to make connections between the 2X, 4X and 8X-tables. Understand that multiplication can be undertaken by partitioning numbers, e.g. 12 X 4 = 10 X 4 + 2 X 4 Introduce the structure of scaling: e.g. Find a ribbon that is 4 times as long as the blue ribbon 2cm 8cm	Recall odd and even numbers to 100 in reference to structured apparatus. Recall and use multiplication facts for the 2X, 3X, 4X, 5X, 8X and 10X tables.	Relate multiplying a 2-digit by 1-digit number using repeated addition and arrays to represent:	Children use an empty number line to chunk efficiently: 4 X 12 = 48 4 X 10 = 40 4 X 2 = 8 3 X 13 = 39 X 10 3 7 X 13 = 91 X 7 70 21
Stage 4:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 7s, 8s, 10s, 25s and 1000s from zero. Count up	Derive factor pairs of numbers using models and images, e.g. Know what happens when a	Recall & use multiplication facts for all times-tables up to 12 X 12.	Relate multiplying a 3/2-digit by 1- digit number with arrays towards using long/short multiplication:	Relate multiplying a 3/2-digit by 1-digit number, now also setting it out as short multiplication. X 10 3 3 7 70 21 21 3 3 3 3 3 3 3 3 3

Stago	and down in tenths and hundredths.	number is multiplied by zero or one. Use reordering to multiply three numbers.	Recall & use	Polato multiplying	7 X 10 = 70 7 X 3 = 21 = 91 At this stage, the non-statutory guidance in the national curriculum suggests teaching short multiplication; however, the team feel that an expanded form of calculation (as set out above) is be a better lead into long/short multiplication.
Stage 5:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 25s and 1000s from zero.	Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.	multiplication facts for all times-tables up to 12 X 12.	Relate multiplying a 4/3/2-digit by 1/2-digit number with grid to using long multiplication:	10 100 80 3 30 24 18 X13 24 30 80 100 234
Stage 6:	Consolidate all previous counting, including forwards and backwards in fractions.	Perform mental calculations, including with mixed numbers and operations.	Recall & use multiplication facts for all times-tables up to 12 X 12. In addition, use facts confidently to make larger calculations.	Relate multiplying a 4/3/2-digit by 1/2-digit number with grid to using short multiplication:	10 8 100 80 3 30 24 18 X13 54 2 180 234

Division:

	Counting	Mental strategies	Rapid	Written calculation and appropriate models and images to	
			recall	support conceptual understanding	
Stage	Count	Doubling up to six and then	Derive/recall	Developing early	Use objects, pictorial representations and arrays to
1:	forwards	ten whilst using related	doubles up	conceptual	show the concept of division as grouping and
	and	models and images.	to five and	understanding of	sharing.
	backwards		derive/recall	division as	
	in 2s, 5s		halves up to	grouping and	
	and 10s		ten.	sharing:	
			Recall odd		
			and even		
			numbers to		
			10 in		
			reference to		"Two children share six pencils between them"
			structured		
			apparatus.		

			3		"Six children are asked to get into three equal
					groups"
			2233		
Stage	Count	Begin to understand and use	Derive/recall	Understanding	Number lines and arrays:
2:	forwards	inverse number operations.	doubles up	division as	$12 \div 3 = 4$
	and	00000	to ten and	repeated	12 + 3 - 4
	backwards	0000	derive/recall	subtraction:	
	in 2s, 3s, 5s		halves up to	 Investigate 	0 1 2 3 4 5 6 7 8 9 10 11 12
	and 10s	15	twenty.	division as	3 3 3
	from zero.			repeated	
			Recall odd	subtraction.	
			and even	 Through 	
		3 90000	numbers to	teacher	

Stage 3:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 8s and 10s from zero.	Stories are used alongside a triad to help children understand links between number operations, e.g. "15 children are asked to get into three groups and find out that there are five people in each group." Use doubling to make connections between the 2X, 4X and 8X-tables. Understand that multiplication can be undertaken by partitioning numbers, e.g. 12 X 4 = 10 X 4 + 2 X 4 Introduce the structure of scaling: e.g. Find a ribbon that is 4 times as long as the blue ribbon.	20 in reference to structured apparatus. Recall and use multiplication facts for the 2X, 5X and 10X-tables. Recall odd and even numbers to 100 in reference to structured apparatus. Recall & use multiplication facts for the 2X, 3X, 4X, 5X, 8X and 10X tables.	modelling, children need to know that division is not commutative. Dividing a 2-digit by 1-digit number, representing this efficiently on a number line:	Children use an empty number line to chunk efficiently. $96 \div 6 = 16$ $6 \times 6 = 36$ $10 \times 6 = 60$ 0 0 0 0 0 0 0
Stage	Counting	2cm 8cm Derive factor pairs of	Recall & use	Dividing a 3/2-	Children use an empty number line to chunk
4:	forwards	numbers using models and	multiplication	digit by 1-digit	efficiently.
	and backwards	images.	facts for all times-tables	number, representing this	224 ÷ 8 = 28
	in 2s, 3s,	Know what happens when a	up to 12 X	efficiently on a	8 x 8 = 64 20 x 8 = 160
	4s, 5s, 7s,	number is multiplied by zero	12.	number line, also	
	8s, 10s, 25s and 1000s	or one.		in relation to long division:	
	from zero.	Use reordering to multiply		 At this stage, 	0 64 224

		three numbers.		no remainders are present unless in a practical context.	28 8 224 - 160 (8 X 20) 20 X 8 = 160 64or 64 - 64 (8 X 8) 8 X 8 = 64 0
Stage 5:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 25s and 1000s from zero.	Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Dividing a 4/3/2-digit by 1-digit number, in relation to long division: • By this stage, there is a statutory requirement that children can use a formal written calculation method, such as long division. • Short division may begin to be taught alongside long division, but still with use of visual representations	As schools have autonomy to decide children's progression in learning between long and short division in Years 5 and 6, the maths team suggest beginning with long division. Remainders should be interpreted in the following ways when long division is used: • as whole numbers • as fractions • through rounding in an appropriate way to the context Long division: 415 ÷ 9 = 46 and 1/9 46 and 1/9 9 415 - 360 (9 X 40) 55 - 54 (9 X 6) 1
Stage 6:	Consolidate all previous counting, including forwards	Perform mental calculations, including with mixed numbers and different number operations.	Recall & use multiplication facts for all times-tables up to 12 X	Dividing a 4/3/2- digit by 2/1-digit number, in relation to long and then short	As schools have autonomy to decide children's progression in learning between long and short division in Years 5 and 6, the maths team suggest moving from long division to short division. Remainders should be interpreted in the following

and backwards in fractions	facts confidently to make larger calculations. there is a statutory requirement that children can use formal writte calculation methods, including lon and short division. Use of visual representation – like the one opposite –	 By this stage, there is a statutory requirement that children can use formal written calculation methods, including long and short division. Use of visual representations – like the ones 	way when short division is used: • through rounding in an appropriate way to the context Long division: 432 ÷ 15 = 28 4/5 2 8 1 5 4 3 2 - 3 0 0 1 3 2 - 1 2 0 1 5×8 Answer: 28 4/5 Answer: 28 4/5
			Short division: $138 \div 6 = 23$ Hundreds Tens Ones 2 3 6 $\sqrt[3]{3}$ 8 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1